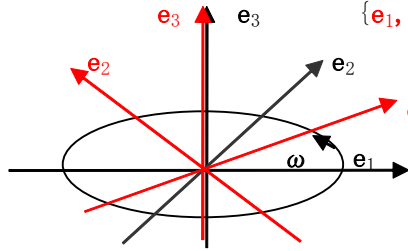


—Coriolis force in view from localized inertia coordinate system—. ' 11/1/22, 7/30

This is entirely **error version**, but shall be left as a wrong sample.

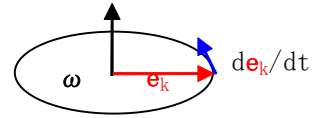
[ 1 ]: Rotational coordinate and deriving "Coriolis Force".

- (1) coordinates:  $\{e_1, e_2, e_3\}$  is inertia fixed coordinate (IC).  
 $\{e_1, e_2, e_3\}$  is non-inertia rotational coordinate (NC)



with angular velocity vector  $\equiv \omega$ .

Then note that  $de_k/dt = \omega \times e_k$ .



(2) position vector:  $R = \sum_{k=1}^3 R_k e_k$ .

(3) velocity vector:

$$V = dR/dt = \sum_{k=1}^3 (dR_k/dt) e_k + \sum_{k=1}^3 R_k (de_k/dt) = \sum_{k=1}^3 (dR_k/dt) e_k + \sum_{k=1}^3 R_k (\omega \times e_k) = \sum_{k=1}^3 V_k e_k + (\omega \times R) = V + (\omega \times R).$$

(4) acceleration vector:

$$f \equiv dV/dt = \sum_{k=1}^3 (dV_k/dt) e_k + \sum_{k=1}^3 V_k (de_k/dt) + (d\omega/dt \times R + \omega \times dR/dt) = \sum_{k=1}^3 (dV_k/dt) e_k + (\omega \times V) + d\omega/dt \times R + \omega \times (V + (\omega \times R)) = dV/dt + 2(\omega \times V) + \omega \times (\omega \times R) + d\omega/dt \times R$$

"in climate science,  $d\omega/dt = 0$ ".

$$f \equiv dV/dt = dV/dt + 2(\omega \times V) + \omega \times (\omega \times R).$$

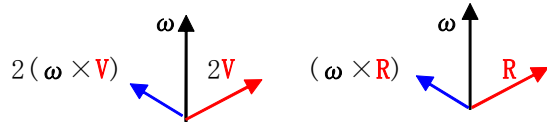
(5)  $f \equiv dV/dt \equiv 0$ , **free motion** in IC and Coriolis force in NC.

$$f \equiv dV/dt \equiv 0. \rightarrow 0 = dV/dt + 2(\omega \times V) + \omega \times (\omega \times R). \rightarrow \underline{dV/dt = -2(\omega \times V) - \omega \times (\omega \times R)}.$$

[ 2 ]: Forcing rotational coordinate as localized? "inertia one" by  $(+\omega \rightarrow -\omega)$ .

Now we must make rotational coordinate (NC) as inertia one by reverse-rotating original fixed coordinate (IC) with angular coordinate  $\omega \equiv -\omega$ . Then we derive

(1)  $dV/dt = 2(\omega \times V) - \omega \times (\omega \times R)$ .

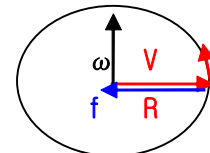


(2) becoming reasonable circular motion (**centrifugal force**):

$$V \equiv 0, V \equiv \omega \times R.$$

$$dV/dt = 2(\omega \times V) - \omega \times (\omega \times R) = \omega \times V = \omega \times (\omega \times R) = f/m.$$

The force **f** must be oriented toward rotational center axis.



(3) If we took the former formulation as  $dV/dt = -2(\omega \times V) - \omega \times (\omega \times R)$ ,

then the circular motion encounter **an evident fatal contradiction !**.

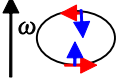
$$dV/dt = -3\omega \times V = -3\omega \times (\omega \times R). \ll \text{it can not be centrifugal force !!!} \gg$$

(4) Author himself noticed the error force direction in Coriolis one in a lecture on climate science and then in my texts on classical mechanics.

(a) the former one (error).

$$\mathbf{f}_C = -2(\boldsymbol{\omega} \times \mathbf{V})_0$$

(b) counter clockwise in typhoon eddy direction in the northern hemisphere.

$$\mathbf{f}_C = +2(\boldsymbol{\omega} \times \mathbf{V})_0$$


<<counter clockwise eddy in NH>>

(c) Rotational axis can not be mathematically regular at  $R = \infty$ .

Pseudo rotating this universe seems more non-regular, though it might be regular in localized time and space.

### Discussion:

In the special theory of relativity, physical basic equation must be invariant by Lorentz transform between "inertia coordinates of uniform motion". At least, a coordinate representing physical law must be **localized inertia one**<sup>(1)</sup>. Because accelerated coordinate such as rotational one is not inertia one, so it seems not absurd that globally accelerated coordinate system would encounter some contradiction or difficulty.

### Reference:

(1) R. Utiyama, Invariant theoretical interpretation of interaction,

Phys. Rev **101** (1956) 1957.

\*The gravitational field theory derived from localized Lorentz invariant principle could conclude the unified field theory (electromagnetic, weak, strong, and gravitational field in elementary particle theory) of  $S_0(11,1)$ <sup>(2)</sup> in 1995 <completion of the theory>.

(2) Authors website.

[http://www.777true.net/GRAVITY\\_FIELD\\_as\\_GUAGE\\_one.pdf](http://www.777true.net/GRAVITY_FIELD_as_GUAGE_one.pdf)

<http://www.777true.net/QFTstructure1.pdf>

**Supplement:** On localized (infinitesimal) inertia coordinate system (2011/1/23).

Any translation accelerating infinitesimal time and space system of  $[ct, x_1, x_2, x_3] \sim [c(t+dt), x_1+dx_1, x_2+dx_2, x_3+dx_3]$  could be considered inertia one. Then rotation is also negligible because of zero rotation radius. The essence is linearization.